

# **$\alpha$ -WISKUNDE**

**Alpha Wiskunde Graad 9 / Alpha Mathematics Grade 9**  
**Finale eksamen 2019 / *Final examination 2019***

## **MEMORANDUM**

**Totaal / *Total*: 100 punte / *marks***

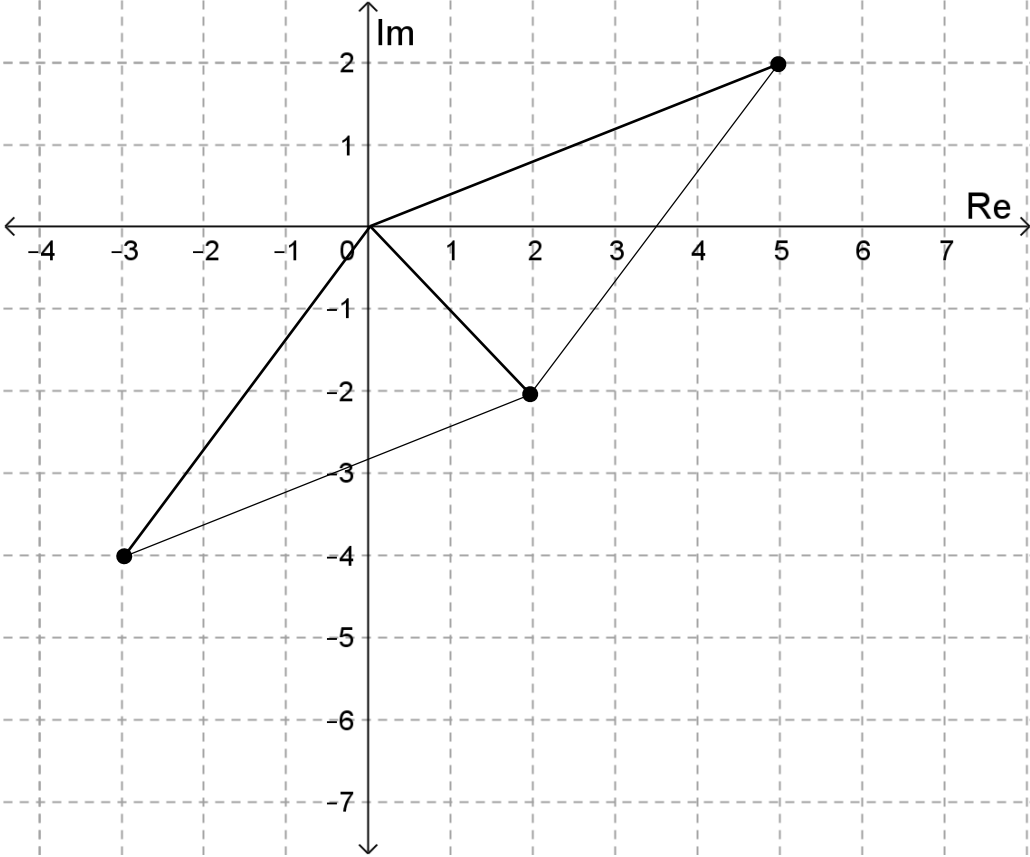
**Hierdie memorandum bestaan uit 7 bladsye. /**  
***This memorandum consists of 7 pages.***

**Vraag / Question 1****[10 punte / marks]**

<b>NR. NO</b>	<b>ANTWOORD ANSWER</b>	<b>PUNTE MARKS</b>
1.1	B	1
1.2	C	1
1.3	A	1
1.4	C	1
1.5	D	1
1.6	A	1
1.7	C	1
1.8	D	1
1.9	C	1
1.10	B	1

Vraag / Question 2

[15 punte / marks]

NR / NO	ANTWOORD / ANSWER	PUNTE / MARKS
2.1.1	$a^2 = (3 - 2i)(3 - 2i)$ $= 9 - 12i + 4i^2$ $= 9 - 12i - 4$ $= 5 - 12i$	✓ Produk ✓ Vereenvoudig ✓ Antwoord [3 punte / marks]
2.1.2	$-(2 + 3i) + 2(3 - 2i)$ $= -2 - 3i + 6 - 4i$ $= 4 - 7i$	✓ Substitusie ✓ Produk ✓ Antwoord [3 punte / marks]
2.1.3	$\frac{2 + 3i}{i} \times \frac{i}{i}$ $= \frac{2i + 3i^2}{i^2}$ $= \frac{2i - 3}{-1}$ $= 3 - 2i$	✓ $\times \frac{i}{i}$ ✓ $i^2 = -1$ ✓ Antwoord [3 punte / marks]
2.1.4	$a^* = 3 + 2i$	✓ Antwoord [1 punt / mark]
2.2	 <p>The diagram shows a complex plane with a horizontal real axis (Re) and a vertical imaginary axis (Im). The real axis is labeled from -4 to 7, and the imaginary axis is labeled from -7 to 2. A triangle is drawn with vertices at the origin (0,0), at (5,2), and at (-3,-4). The points are marked with solid black dots, and the lines connecting them are solid black lines.</p>	✓ (5; 2) ✓ (-3; -4) ✓ (2; -2) ✓ Vorm [4 punte / marks]
2.3	$\sqrt{-49} = 7i$	✓ Antwoord [1 punt / mark]

**Vraag / Question 3**
**[9 punte / marks]**

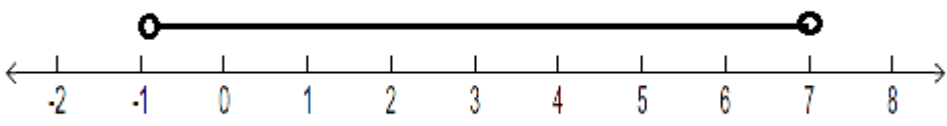
NR / NO	ANTWOORD / ANSWER	PUNTE / MARKS												
3.1.1	$(1)^3 - 2(1)^2 - 5(1) + 6$ $= 0$	✓ Vervang 1 in ✓ Antwoord [2 punte / marks]												
3.1.2	<table style="border-collapse: collapse; margin-left: auto; margin-right: auto;"> <tr> <td style="border-right: 1px solid black; padding: 5px;">1</td> <td style="padding: 5px;">1</td> <td style="padding: 5px;">-1</td> <td style="padding: 5px;">-6</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"></td> <td style="padding: 5px;">1</td> <td style="padding: 5px;">-2</td> <td style="padding: 5px;">-5</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"></td> <td style="padding: 5px;">1</td> <td style="padding: 5px;">-1</td> <td style="padding: 5px;">-6</td> </tr> </table> $\therefore x^3 - 2x^2 - 5x + 6$ $= (x - 1)(x^2 - x - 6)$ $= (x - 1)(x - 3)(x + 2)$	1	1	-1	-6		1	-2	-5		1	-1	-6	✓ Methode ✓ $(x^2 - x - 6)$ ✓ $(x - 3)$ ✓ $(x + 2)$ [4 punte / marks]
1	1	-1	-6											
	1	-2	-5											
	1	-1	-6											
3.2	$5x^4 - 80y^4$ $= 5(x^4 - 16y^4)$ $= 5(x^2 + 4y^2)(x^2 - 4y^2)$ $= 5(x^2 + 4y^2)(x + 2y)(x - 2y)$	✓ Haal 5 uit ✓ Verskil van vierkante ✓ Antwoord [3 punte / marks]												

**Vraag / Question 4**
**[11 punte / marks]**

NR / NO	ANTWOORD / ANSWER	PUNTE / MARKS
4.1	$125^{\frac{2}{3}}$ $= (5^3)^{\frac{2}{3}}$ $= 5^2$	✓ Priemfaktore ✓ $5^2$ [2 punte / marks]
4.2	$81 \times 3^{-5}$ $= 3^4 \times 3^{-5}$ $= 3^{-1}$ $= \frac{1}{3}$	✓ Priemfaktore ✓ $3^{-1}$ ✓ Antwoord [3 punte / marks]
4.3	$\frac{2 \cdot 6^2 + 4 \cdot 6^2}{6^2}$ $= \frac{6 \cdot 6^2}{6^2}$ $= 6$	✓ Vereenvoudig ✓ Antwoord [2 punte / marks]
4.4	$8^2 + 3 \cdot 4^3$ $= (2^3)^2 + 3 \cdot (2^2)^3$ $= 2^6 + 3 \cdot 2^6$ $= 4 \cdot 2^6$ $= 2^2 \cdot 2^6$ $= 2^8$	✓ Priemfaktore ✓ Vereenvoudig ✓ Vereenvoudig ✓ Antwoord [4 punte / marks]

Vraag / Question 5

[10 punte / marks]

NR / NO	ANTWOORD / ANSWER	PUNTE / MARKS
5.1	$-3 2 - 6 $ $= -3 -4 $ $= -3(4)$ $= -12$	✓ Vereenvoudig ✓ 4 ✓ Antwoord <b>[3 punte / marks]</b>
5.2	$ 3x - 2  = 4$ $3x - 2 = 4$ of $3x - 2 = -4$ $3x = 6$ $3x = -2$ $x = 2$ $x = \frac{-2}{3}$	✓ ✓ Albei vergelykings ✓ ✓ Antwoorde <b>[3 punte / marks]</b>
5.3.1		✓ Oop kol by -1 ✓ Oop kol by 7 <b>[2 punte / marks]</b>
5.3.2	$-1 < x < 7$	✓ ✓ Antwoord <b>[2 punte / marks]</b>

Vraag / Question 6

[11 punte / marks]

NR / NO	ANTWOORD / ANSWER	PUNTE / MARKS
6.1	$Tan225^\circ = 1$	✓ Antwoord <b>[1 punt / mark]</b>
6.2	$Tan\theta = \frac{12}{10}$ $\theta \approx 50^\circ$	✓ $\frac{12}{10}$ ✓ Antwoord <b>[2 punte / marks]</b>
6.3	$Cos60^\circ = \frac{OB}{2}$ $OB = 2Cos60^\circ$ $OB = 1$ $B(1; 0)$	✓ Verhouding ✓ Vereenvoudig ✓ Antwoord <b>[3 punte / marks]</b>
6.4	$Sin30^\circ = \frac{h}{100}$ $h = 50m$	✓ Antwoord <b>[1 punt / mark]</b>
6.5.1	$Tan42^\circ = \frac{CD}{15}$ $CD = 14m$	✓ Antwoord <b>[1 punt / mark]</b>
6.5.2	$Tan35^\circ = \frac{14}{AD}$ $AD = \frac{14}{Tan35^\circ}$ $AD \approx 20m$	✓ Vereenvoudig ✓ AD

NR / NO	ANTWOORD / ANSWER	PUNTE / MARKS
	$AB = 15 + 20$ $AB = 35m$	✓ Antwoord <b>[3 punte / marks]</b>

**Vraag / Question 7**

**[10 punte / marks]**

NR / NO	ANTWOORD / ANSWER	PUNTE / MARKS
7.1	$26 \times 26 \times 26 \times 10 \times 10 \times 10$ $= 17\,576\,000$	✓ Metode ✓ Antwoord <b>[2 punte / marks]</b>
7.2	$26 \times 25 \times 24 \times 10 \times 9 \times 8$ $= 11\,232\,000$	✓ Metode ✓ Antwoord <b>[2 punte / marks]</b>
7.3	$5 \times 25 \times 24 \times 10 \times 9 \times 8$ $= 2\,160\,000$	✓ 5 ✓ Metode ✓ Antwoord <b>[3 punte / marks]</b>
7.4	$26 \times 25 \times 24 \times 5 \times 9 \times 8$ $= 5\,616\,000$	✓ 5 ✓ Metode ✓ Antwoord <b>[3 punte / marks]</b>

**Vraag / Question 8**

**[10 punte / marks]**

NR / NO	ANTWOORD / ANSWER	PUNTE / MARKS
8.1	$30x + 15y \leq 480$ $2x + y \leq 32$	✓ $30x + 15y$ ✓ 480 ✓ Vereenvoudigde antwoord <b>[3 punte / marks]</b>

NR / NO	ANTWOORD / ANSWER	PUNTE / MARKS
8.2		<ul style="list-style-type: none"> <li>✓ Skets van ongelijkheid 1</li> <li>✓ Skets van ongelijkheid 2</li> <li>✓ Gangbare gebied</li> </ul> <p style="text-align: right;"><b>[3 punte / marks]</b></p>
8.3	$P = 40(0) + 50(16) = 800$ $P = 40(16) + 50(0) = 640$ $P = 40(12) + 50(8) = 880$ Maksimum wins is 12 rokke en 8 broeke.	<ul style="list-style-type: none"> <li>✓ Invervanging</li> <li>✓ Invervanging</li> <li>✓ Invervanging</li> <li>✓ Antwoord</li> </ul> <p style="text-align: right;"><b>[4 punte / marks]</b></p>

**Vraag / Question 9**

**[14 punte / marks]**

NR / NO	ANTWOORD / ANSWER	PUNTE / MARKS																									
9.1	$a^3 + 2a^2b - b^3 \neq (a - b)(a^2 + ab - b^2)$ $a^3 + 2a^2b - b^3 \neq a^3 + 2a^2 - b^3$ $0 \neq 0$ Wat onwaar is daarom is die bewering waar.	<ul style="list-style-type: none"> <li>✓ Negering</li> <li>✓ Vereenvoudig</li> <li>✓ <math>0 \neq 0</math></li> <li>✓ Gevolgtrekking</li> </ul> <p style="text-align: right;"><b>[4 punte / marks]</b></p>																									
9.2	<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th></th> <th>Stelling A</th> <th>Teenoorgestelde stelling A'</th> <th>Waar</th> <th>Onwaar</th> </tr> </thead> <tbody> <tr> <td>9.2.1</td> <td><math>\pi \in \mathbb{Q}</math></td> <td><math>\pi \notin \mathbb{Q}</math></td> <td></td> <td>✓</td> </tr> <tr> <td>9.2.2</td> <td>Alle <math>\mathbb{Q}</math> is ook <math>\mathbb{R}</math>.</td> <td>Geen <math>\mathbb{Q}</math> is <math>\mathbb{R}</math> nie.</td> <td>✓</td> <td></td> </tr> <tr> <td>9.2.3</td> <td><math>\frac{25}{5} \geq 7</math></td> <td><math>\frac{25}{5} &lt; 7</math></td> <td></td> <td>✓</td> </tr> <tr> <td>9.2.4</td> <td><math>\frac{13+1}{7} = 2</math></td> <td><math>\frac{13+1}{7} \neq 2</math></td> <td>✓</td> <td></td> </tr> </tbody> </table>		Stelling A	Teenoorgestelde stelling A'	Waar	Onwaar	9.2.1	$\pi \in \mathbb{Q}$	$\pi \notin \mathbb{Q}$		✓	9.2.2	Alle $\mathbb{Q}$ is ook $\mathbb{R}$ .	Geen $\mathbb{Q}$ is $\mathbb{R}$ nie.	✓		9.2.3	$\frac{25}{5} \geq 7$	$\frac{25}{5} < 7$		✓	9.2.4	$\frac{13+1}{7} = 2$	$\frac{13+1}{7} \neq 2$	✓		<ul style="list-style-type: none"> <li>✓ Teenoorgestelde stelling.</li> <li>✓ Waar/ onwaar</li> </ul> <p style="text-align: right;"><b>[8 punte / marks]</b></p>
	Stelling A	Teenoorgestelde stelling A'	Waar	Onwaar																							
9.2.1	$\pi \in \mathbb{Q}$	$\pi \notin \mathbb{Q}$		✓																							
9.2.2	Alle $\mathbb{Q}$ is ook $\mathbb{R}$ .	Geen $\mathbb{Q}$ is $\mathbb{R}$ nie.	✓																								
9.2.3	$\frac{25}{5} \geq 7$	$\frac{25}{5} < 7$		✓																							
9.2.4	$\frac{13+1}{7} = 2$	$\frac{13+1}{7} \neq 2$	✓																								
9.3	Waar, lemoene kos die meeste.	<ul style="list-style-type: none"> <li>✓ ✓ Antwoord</li> </ul> <p style="text-align: right;"><b>[2 punte / marks]</b></p>																									

- EINDE VAN DIE MEMORANDUM / END OF THE MEMORANDUM -